



# Enhanced extraction of weighted networks backbones

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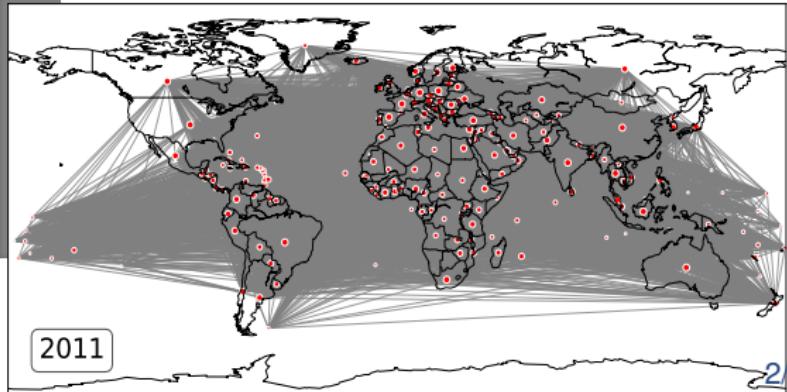
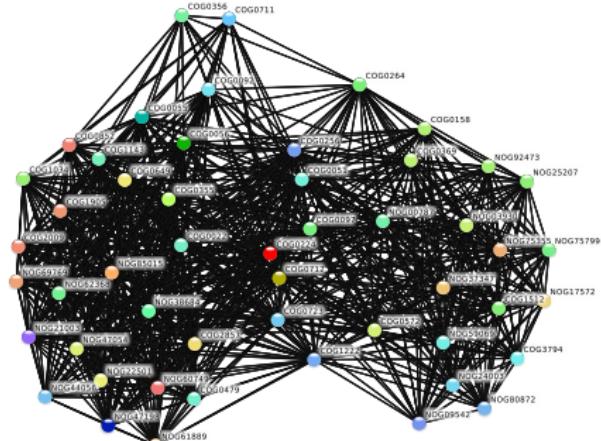
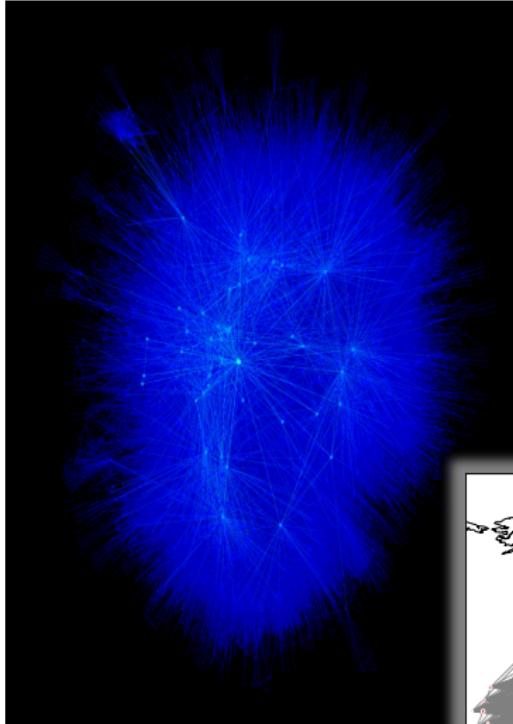
Tuesday 21 March 2017, Complenet 2017, Dubrovnik, Croatia







## Motivation





Question:

What can we **learn** from a complex system whose network representation is **noisy** and/or extremely **dense**?

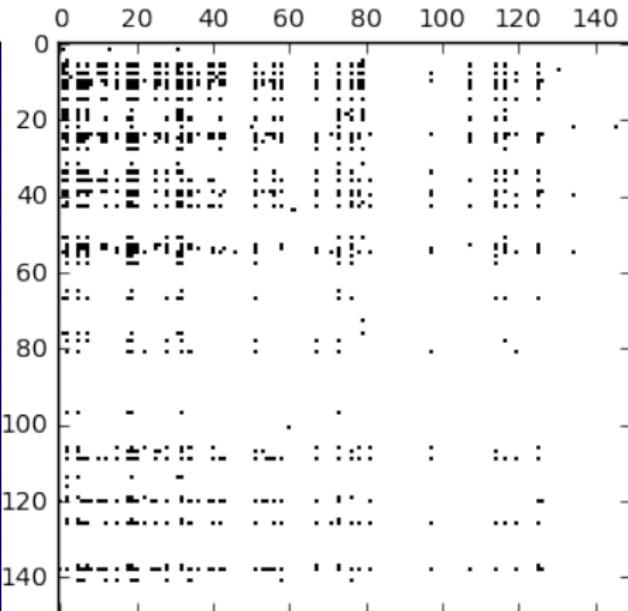
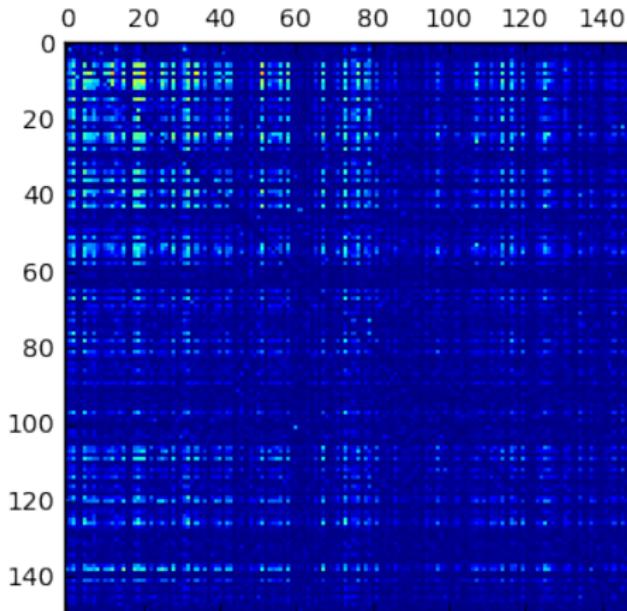
# **BRACE YOURSELVES**



# **FILTERING IS COMING**



# Other methods





The screenshot shows a research article from PLOS Computational Biology. The article title is "A Topological Criterion for Filtering Information in Complex Brain Networks". It is an open access, peer-reviewed research article. The authors listed are Fabrizio De Vico Fallani, Vito Latora, and Mario Chavez. The article was published on January 11, 2017, with the DOI <http://dx.doi.org/10.1371/journal.pcbi.1005305>. The interface includes tabs for Article, Authors, Metrics, Comments, and Related Content.

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RESEARCH ARTICLE

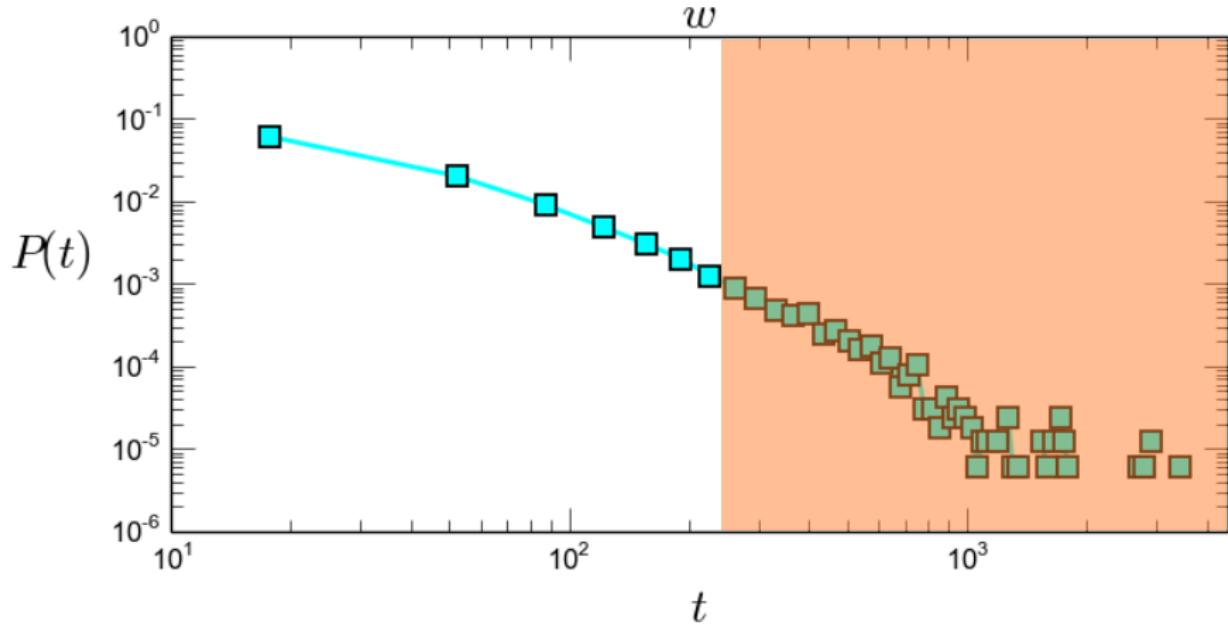
## A Topological Criterion for Filtering Information in Complex Brain Networks

Fabrizio De Vico Fallani, Vito Latora, Mario Chavez

Version 2 Published: January 11, 2017 • <http://dx.doi.org/10.1371/journal.pcbi.1005305>

Article	Authors	Metrics	Comments	Related Content
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- De Vico Fallani F., et al. *A Topological Criterion for Filtering Information in Complex Brain Networks*.  
PLoS Comp. Bio. **13** e1005305 (2017).



- Granovetter, M. S. *The Strength of Weak Ties*. Am. Jour. Soc., **78**, 1360 (1973).



# Other methods

Institution: EPFL

Proceedings of the National Academy of Sciences of the United States of America

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Home > Current Issue > vol. 106 no. 16 > M. Ángeles Serrano, 6483–6488, doi: 10.1073/pnas.0808904106

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## Extracting the multiscale backbone of complex weighted networks

M. Ángeles Serrano<sup>a,1</sup>, Marián Boguñá<sup>b</sup> and Alessandro Vespignani<sup>c,d</sup>

Author Affiliations 

Edited by Peter J. Bickel, University of California, Berkeley, CA, and approved March 2, 2009 (received for review September 9, 2008)

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### Don't Miss

- Serrano M.A., et al. *Extracting the multiscale backbone of complex weighted networks*. Proc. Natl. Acad. Sci. (USA) **106** 6483 (2009).

## PHYSICAL REVIEW E

*statistical, nonlinear, and soft matter physics*

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### Information filtering in complex weighted networks

Filippo Radicchi, José J. Ramasco, and Santo Fortunato

Phys. Rev. E **83**, 046101 – Published 1 April 2011

Article

References

Citing Articles (8)

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#### ABSTRACT

Many systems in nature, society, and technology can be described as networks, where the vertices are the system's elements, and edges between vertices indicate the interactions between the corresponding elements. Edges may be weighted if the interaction strength is measurable. However, the full network information is often redundant because tools and techniques from network analysis

- Radicchi, F., et al. *Information filtering in complex weighted networks*. Physical Review E, **83** 046101. (2011).



## Main Features

1. Based on the comparison between the observed network and a null model one.



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2. Null model: maximum-entropy canonical ensemble of networks satisfying given constraints.



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3. Constraints:  $\{k_i\}$  and  $\{s_i\}$  preserved (on average).

- Mastrandrea, R., et al. *Enhanced reconstruction of weighted networks from strengths and degrees*. New Jour. Phys., **16**, 043022. (2014).



## Main Features

1. Based on the comparison between the observed network and a null model one.
2. Null model: maximum-entropy canonical ensemble of networks satisfying given constraints.
3. Constraints:  $\{k_i\}$  and  $\{s_i\}$  preserved (on average).
4. Two versions: **local** (focus on links) and **global** (focus on entire network).



## Local ECM-filter

1. Generate the null model ensemble and compute:

$$q_{ij}(w) \equiv \frac{(x_i x_j)^{\Theta(w_{ij})} (y_i y_j)^{w_{ij}} (1 - y_i y_j)}{1 - y_i y_j + x_i x_j y_i y_j}.$$



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2. Associate for each link a  $p$ -value,  $\gamma$ , such that  $P(w_{ij} > w_{ij}^*)$ .



## Local ECM-filter

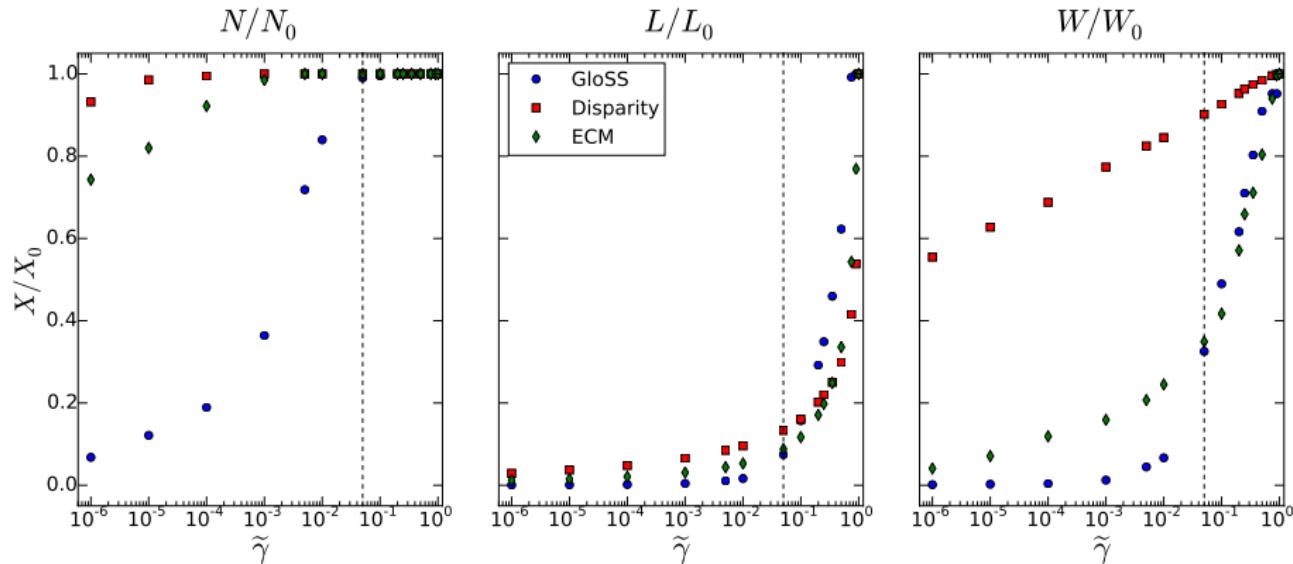
1. Generate the null model ensemble and compute:

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2. Associate for each link a  $p$ -value,  $\gamma$ , such that  $P(w_{ij} > w_{ij}^*)$ .
3. Select a threshold  $\tilde{\gamma}$  and remove all the links with  $\gamma_{ij} > \tilde{\gamma}$ .

# Results

# Comparison among methods





# A serious example . . .

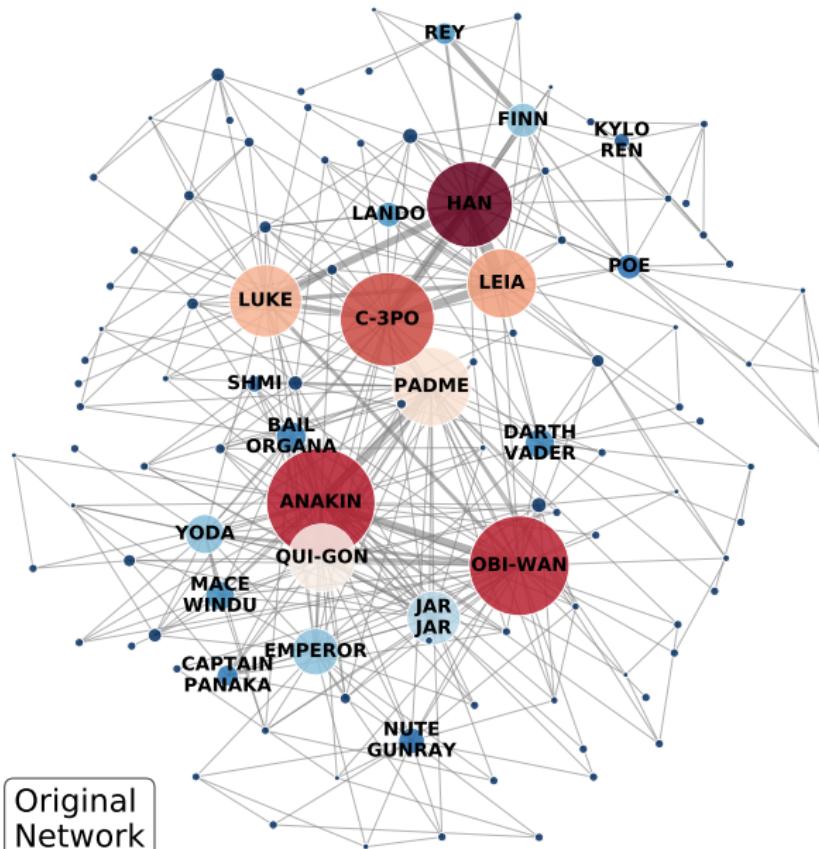


## A serious example ...

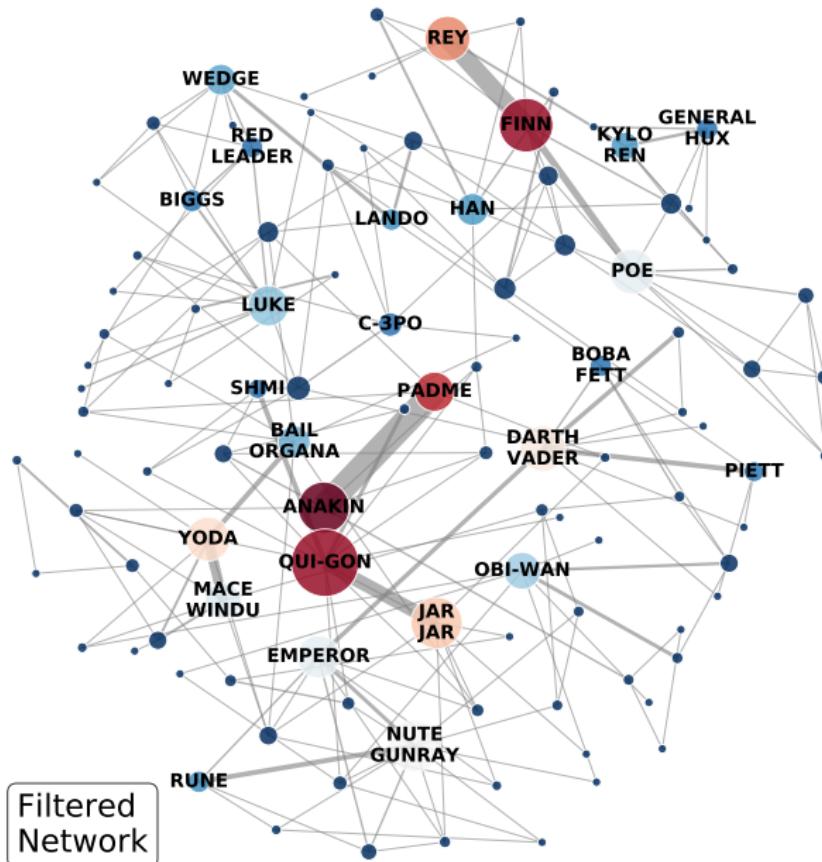
A long time ago in a galaxy far,  
far away....

- <http://evelinag.com/blog/2015/12-15-star-wars-social-network/>

# A serious example . . .



# A serious example . . .



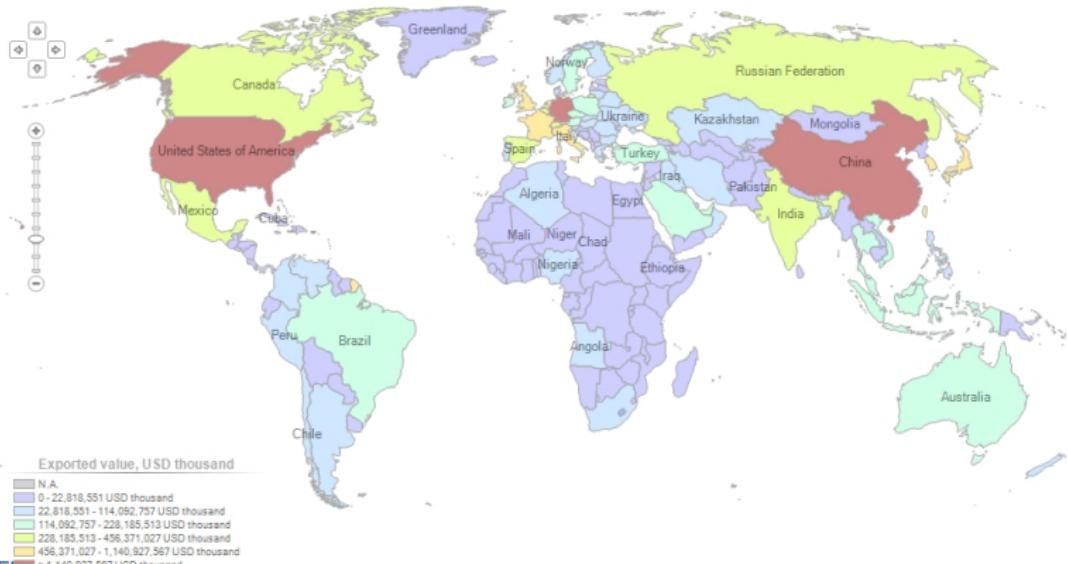
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## International Trade Network 1998 – 2011

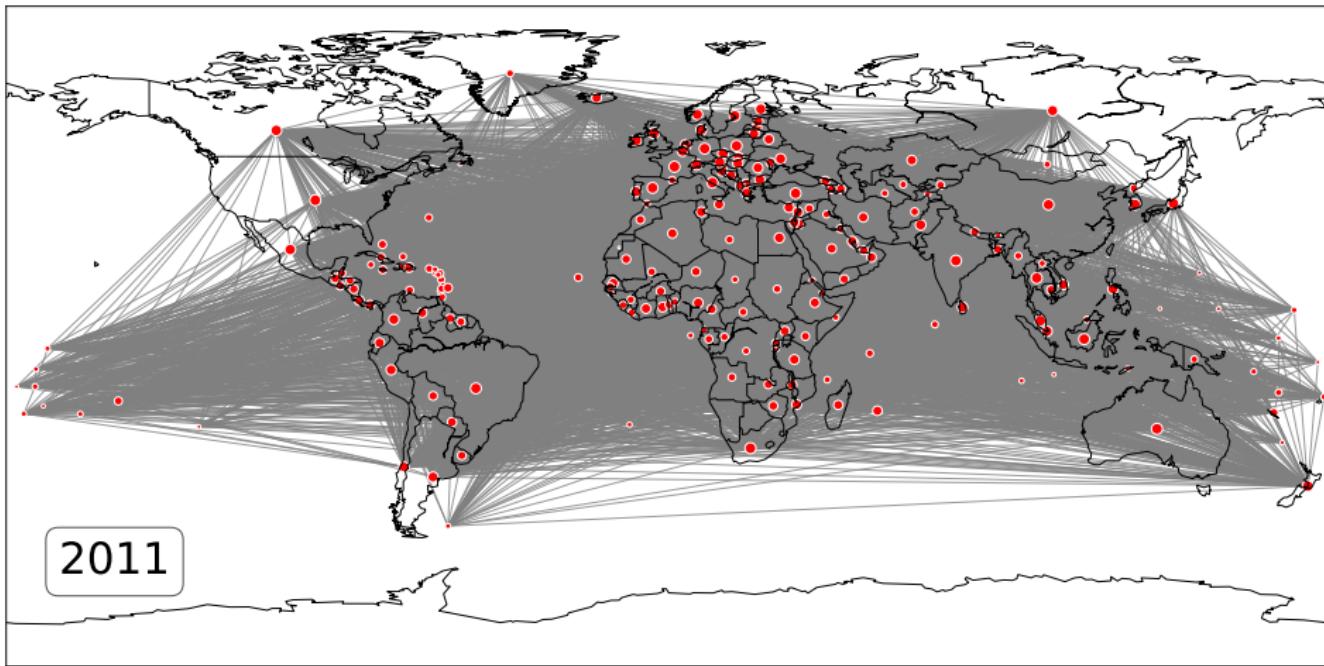


International  
Trade  
Centre

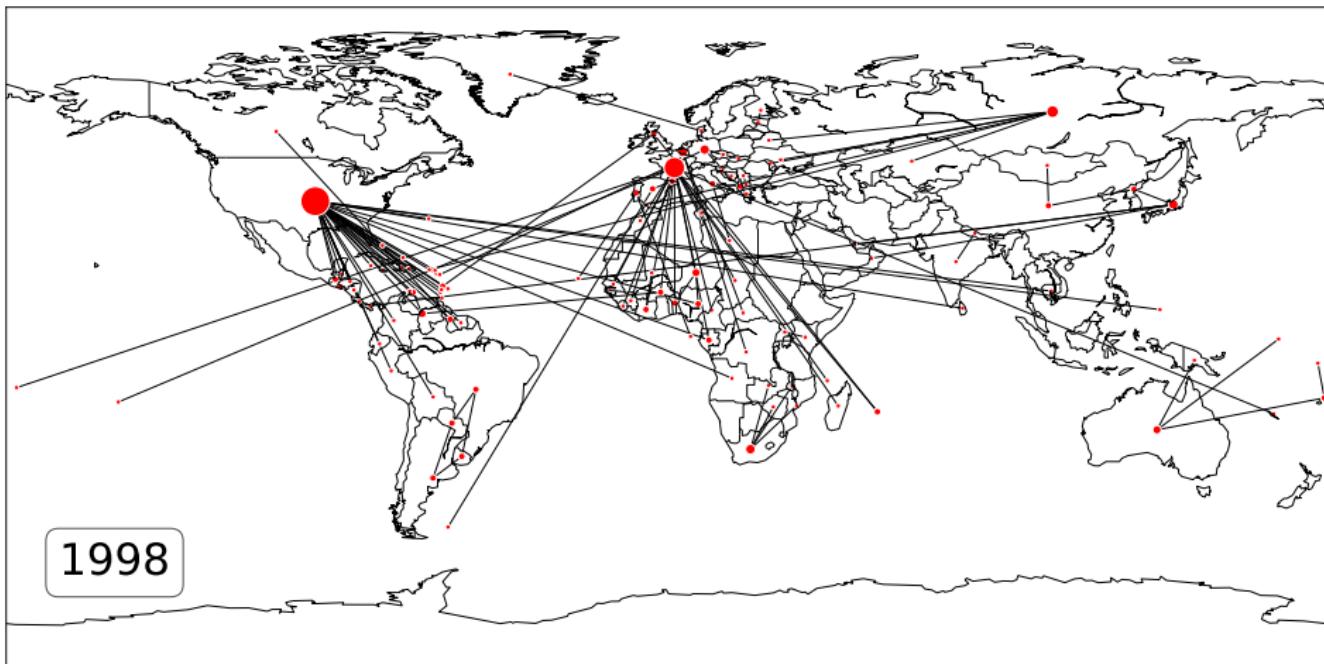
exporting countries for the selected product in 2015  
Product : TOTAL All products



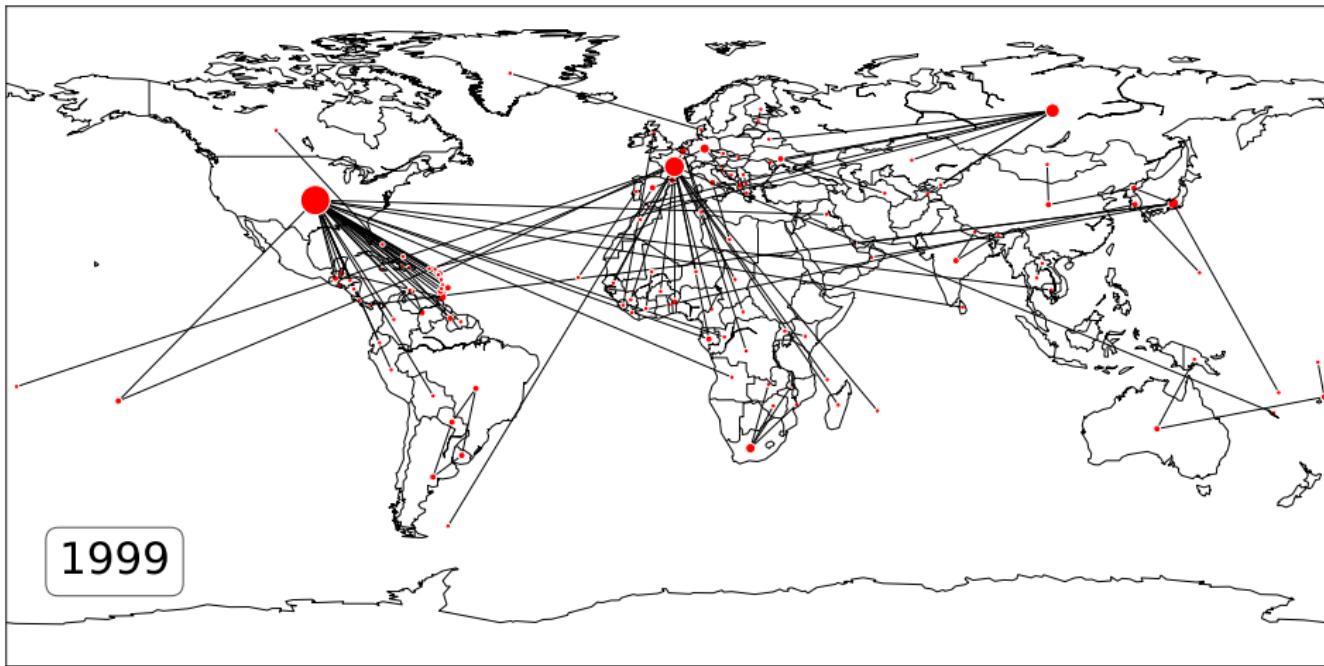
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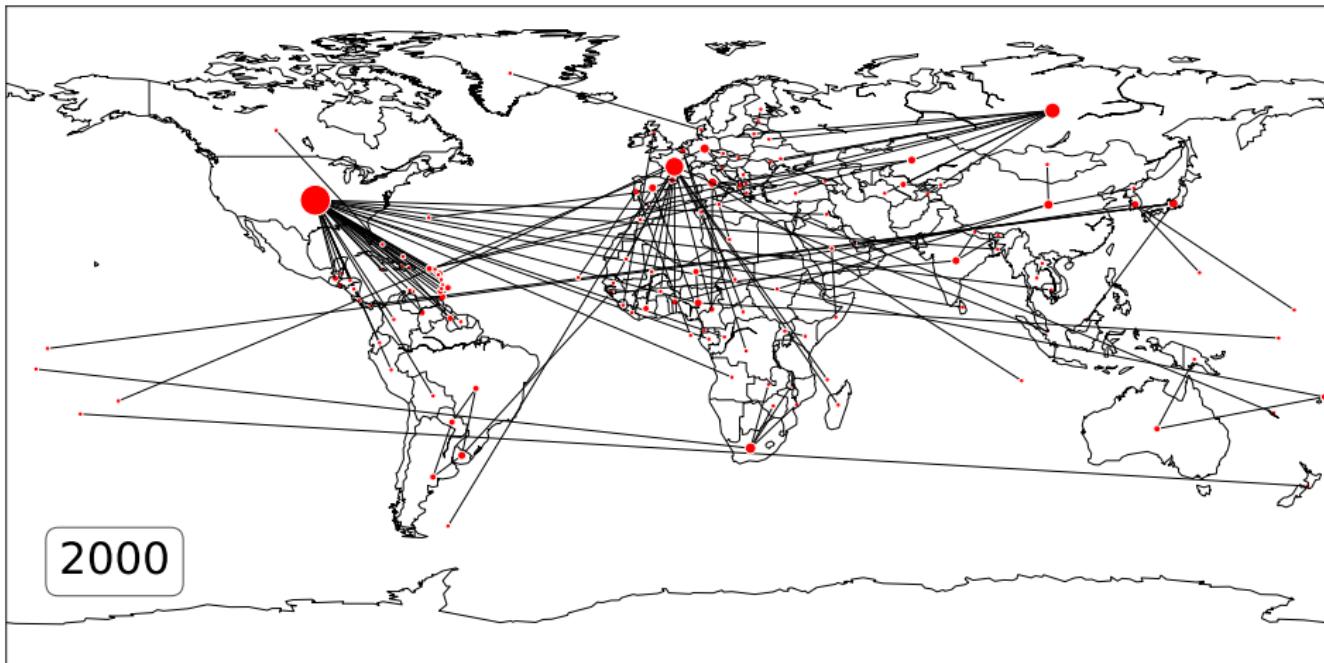
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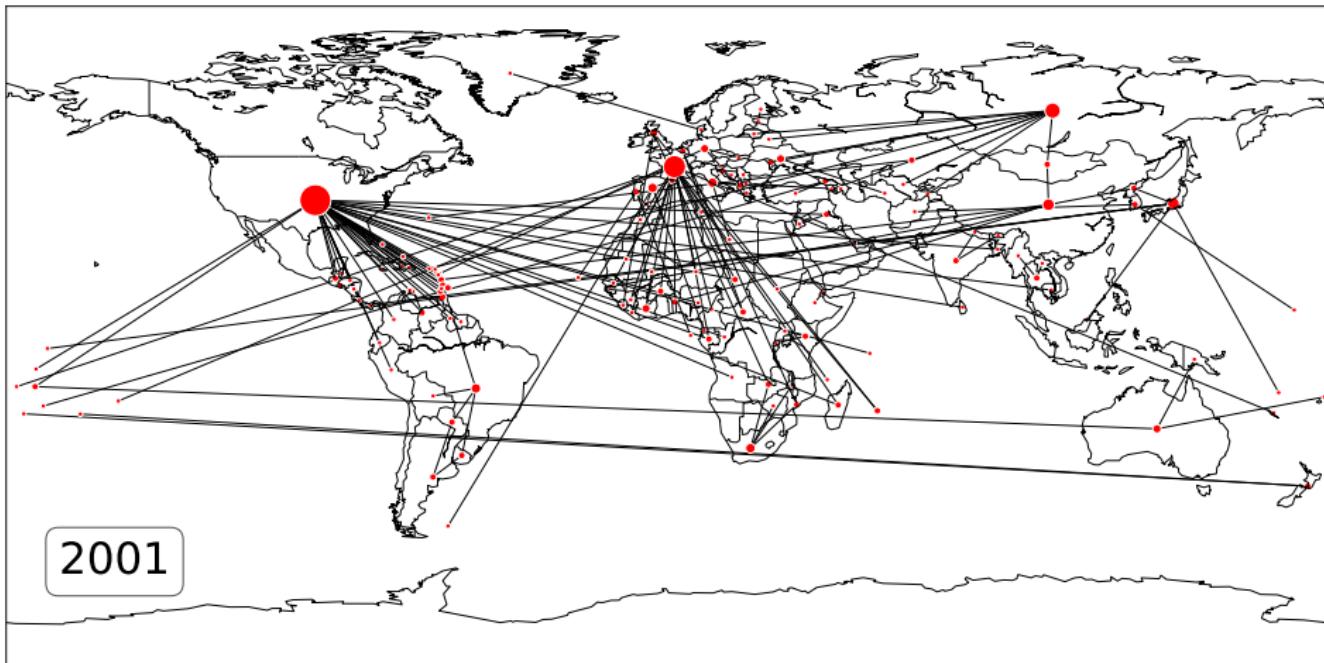
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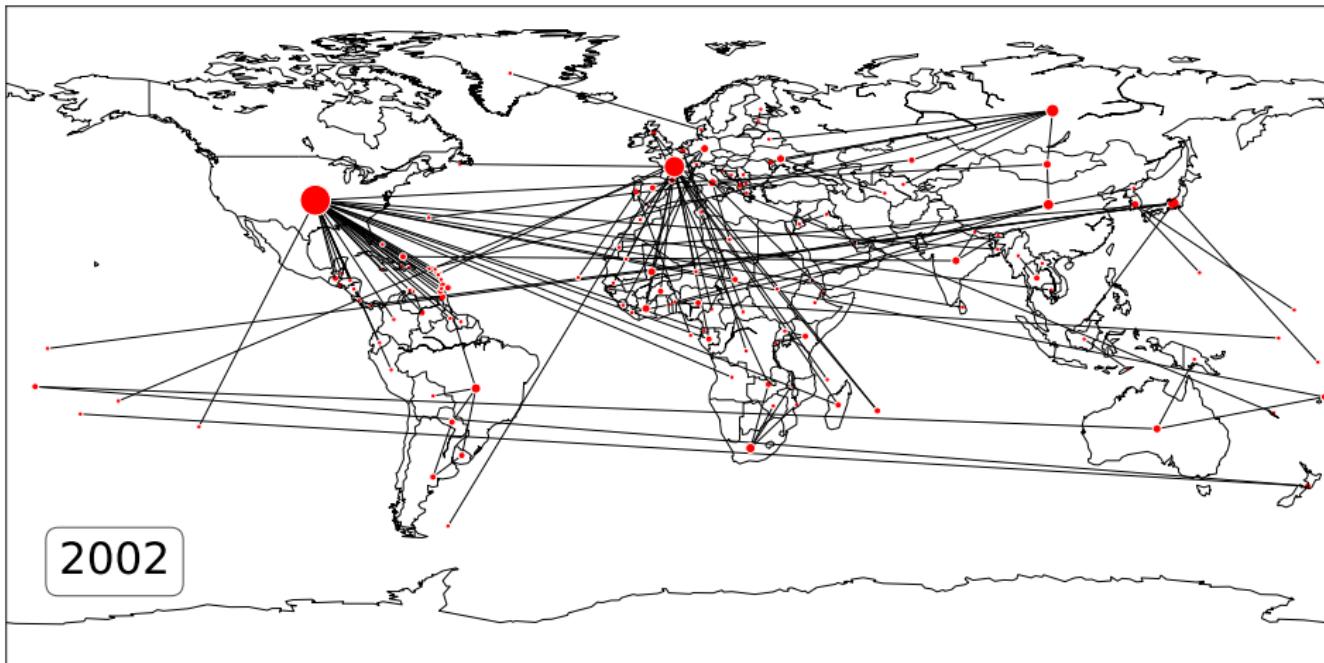
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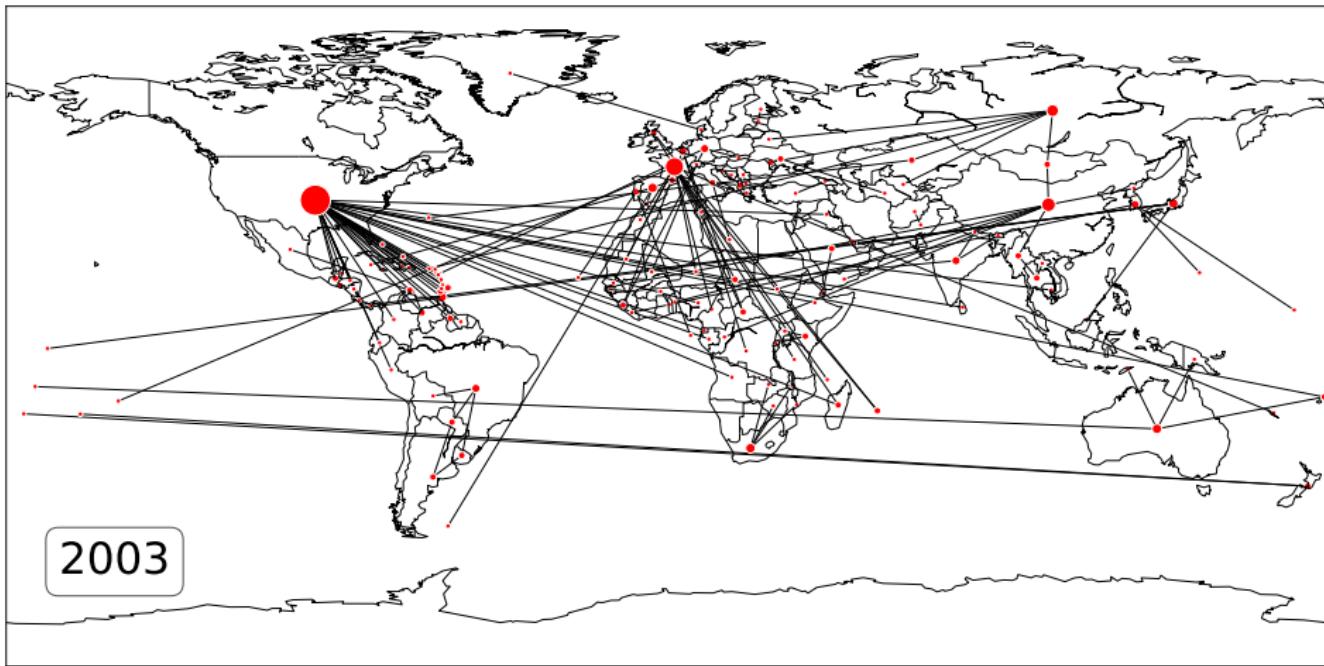
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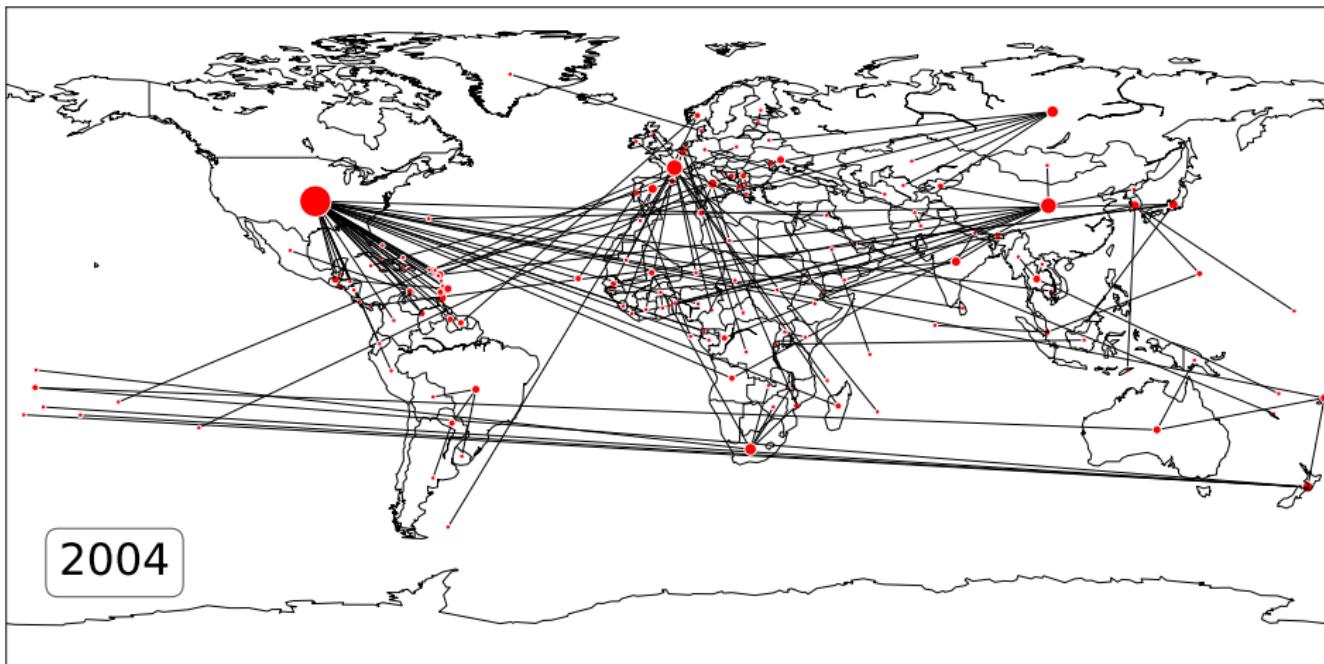
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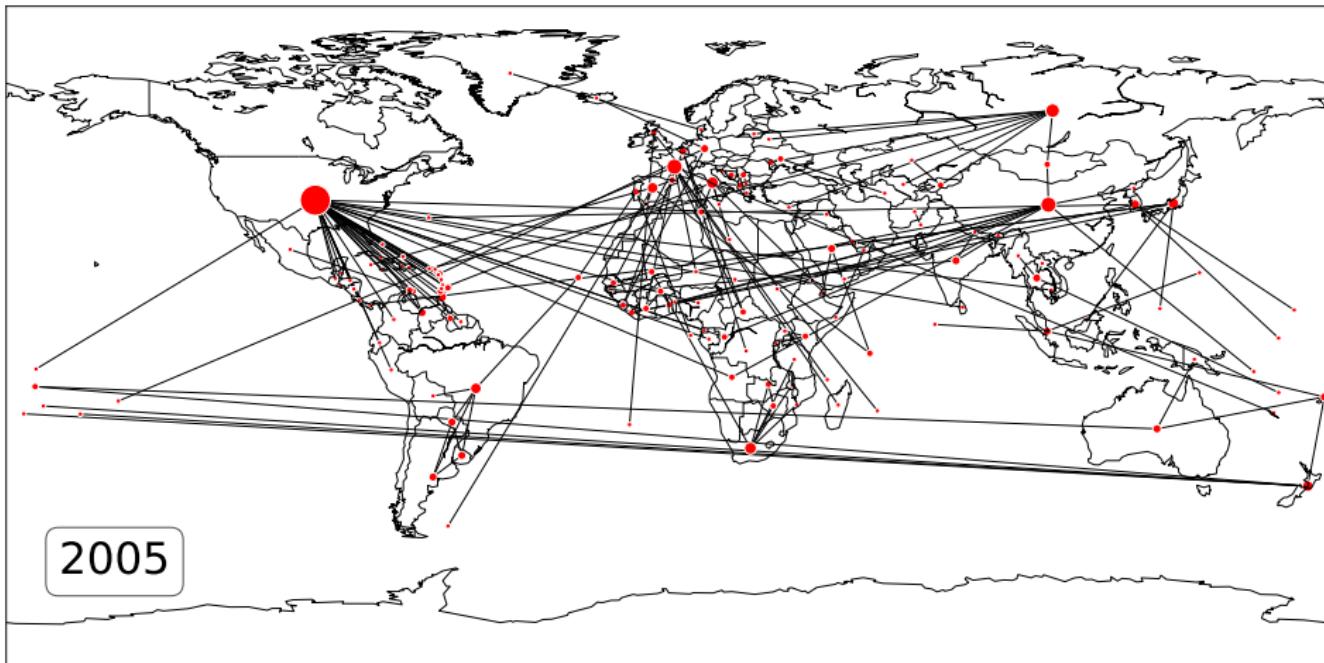
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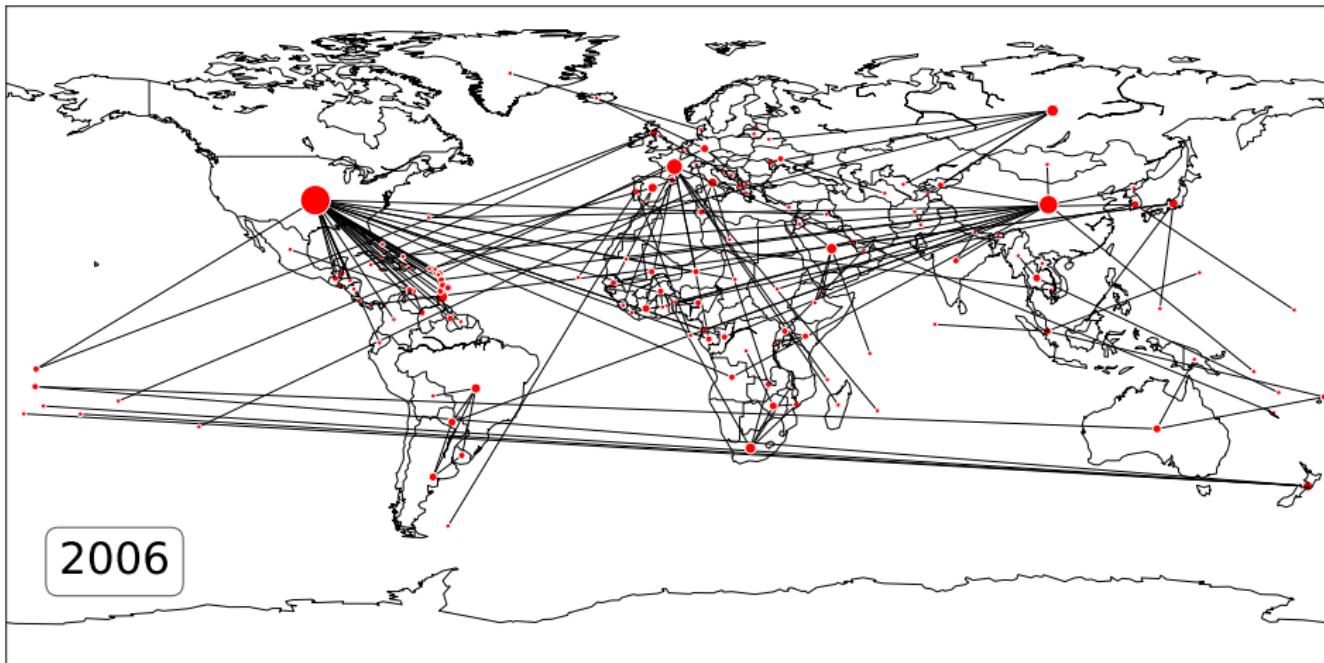
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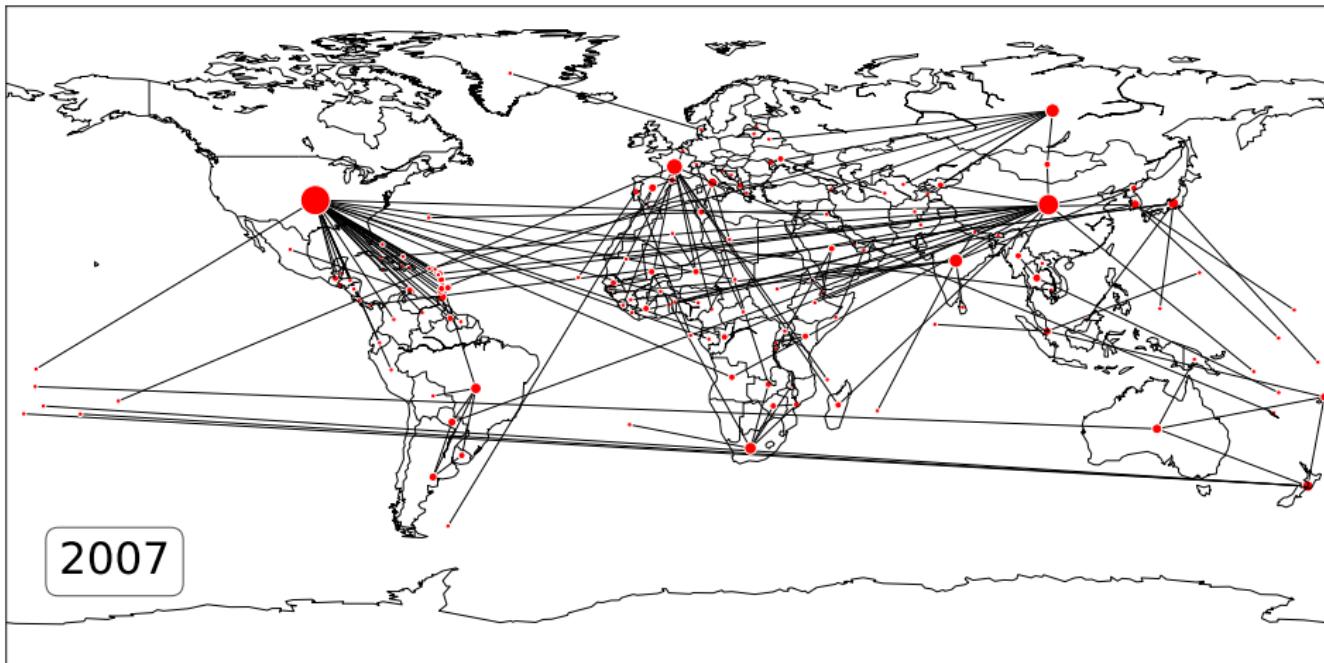
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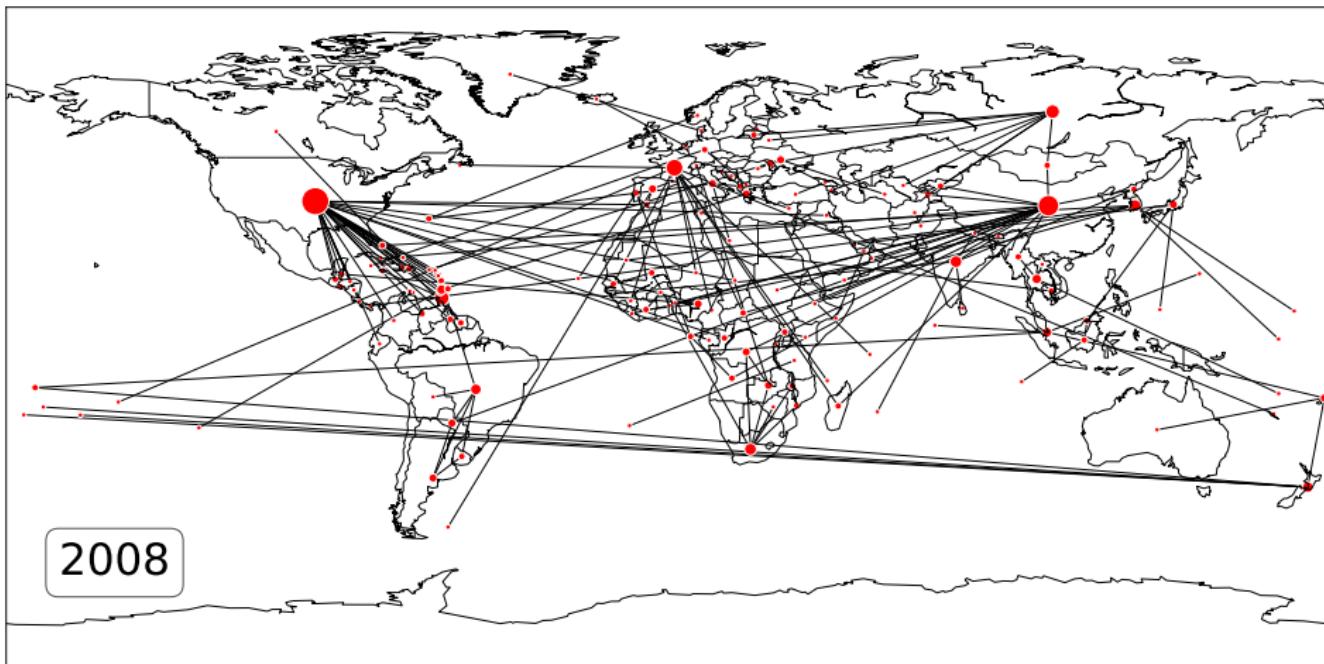
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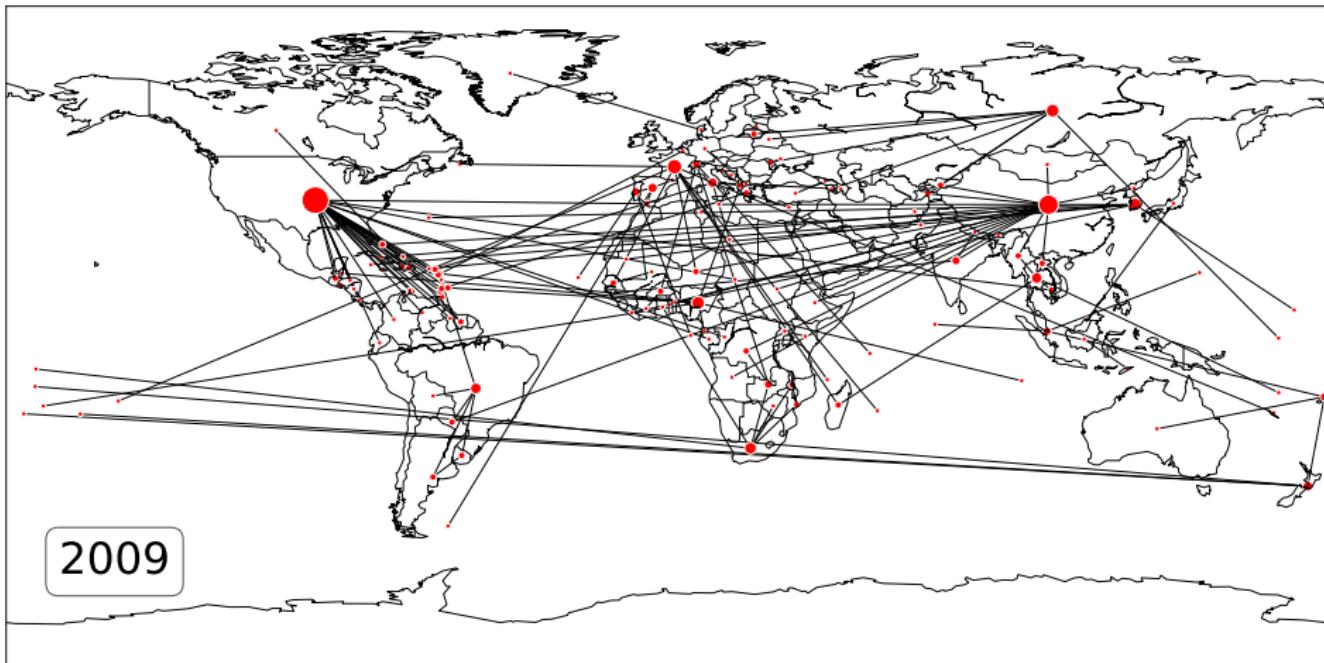
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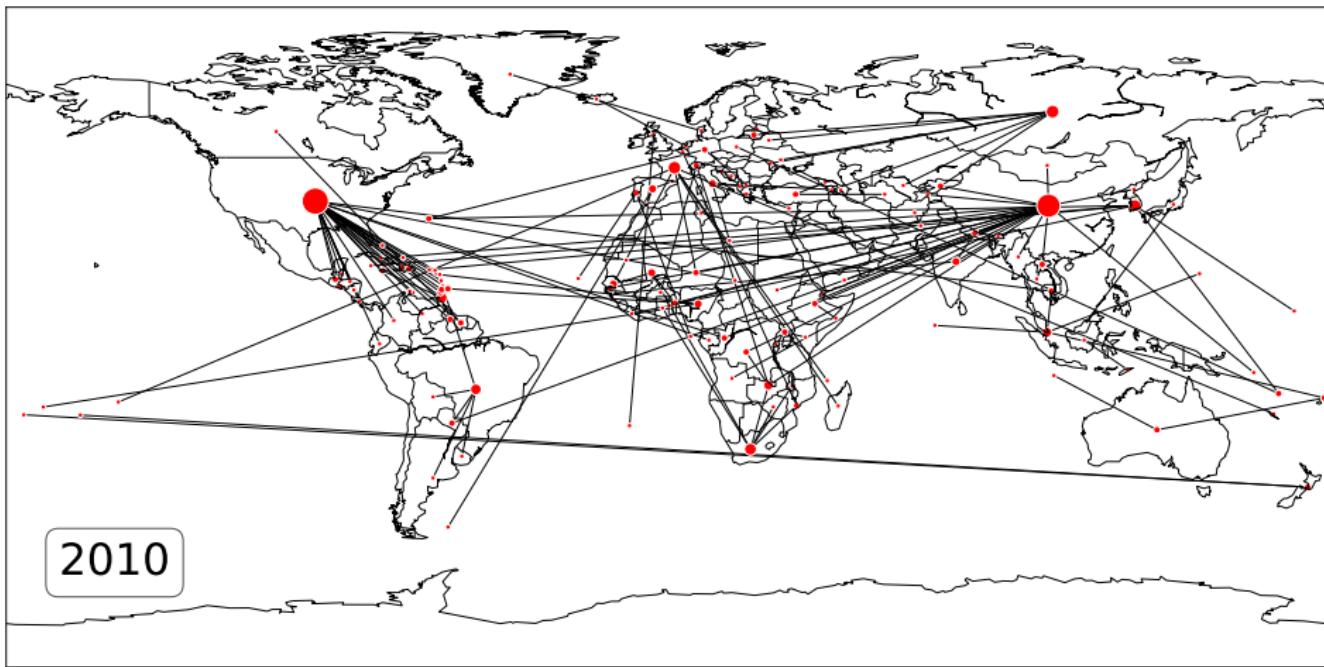
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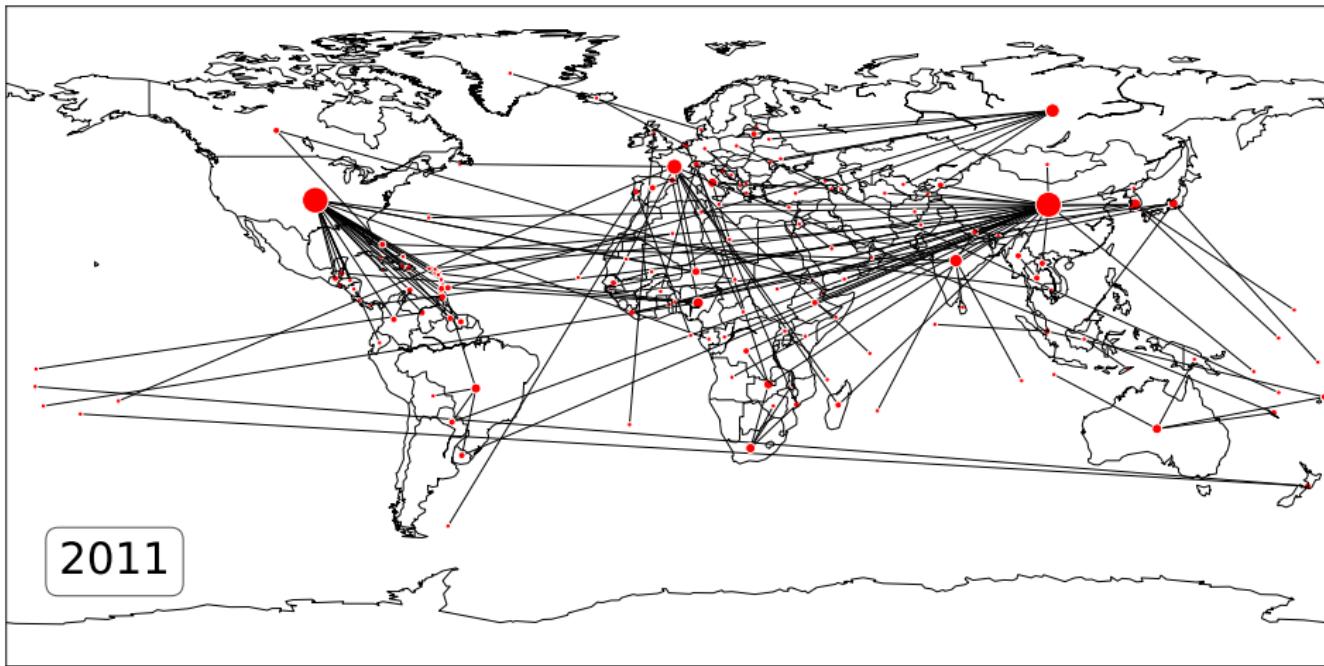
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... and a less serious one



... and a less serious one



# Conclusions

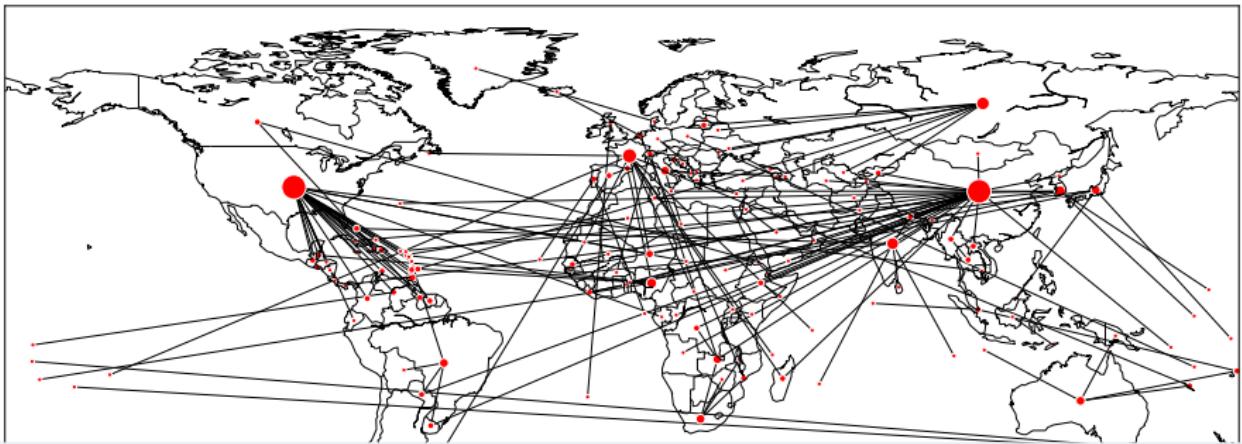


## Take home messages

Filtering is becoming a more and more required step to continue using networks in complex systems.



# Take home messages



ECM filter overcomes limitations of previous approaches and retrieves non trivial features.

# Acknowledgements



**Diego Garlaschelli**



**Valerio Gemmetto**



## Acknowledgements

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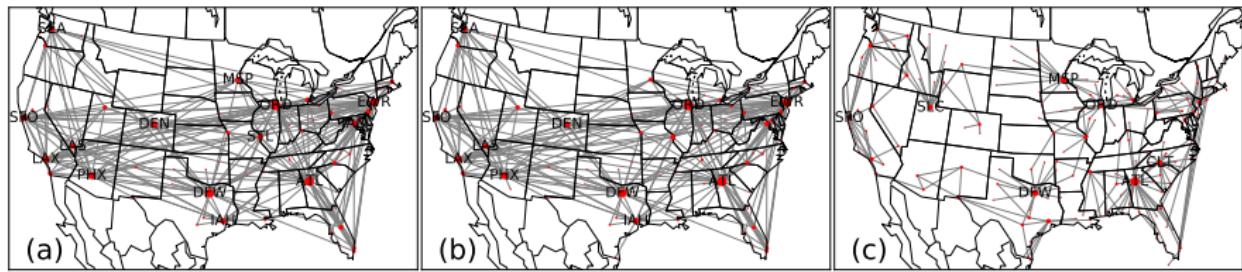
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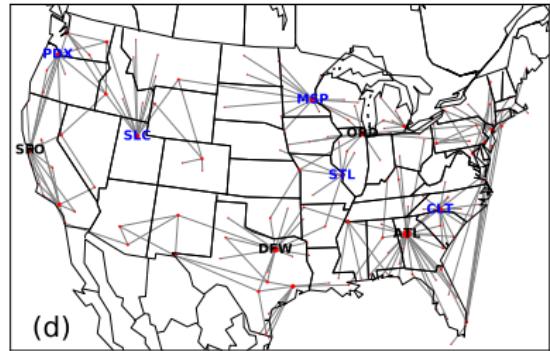
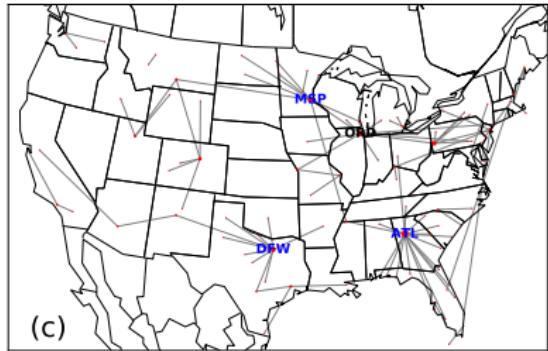
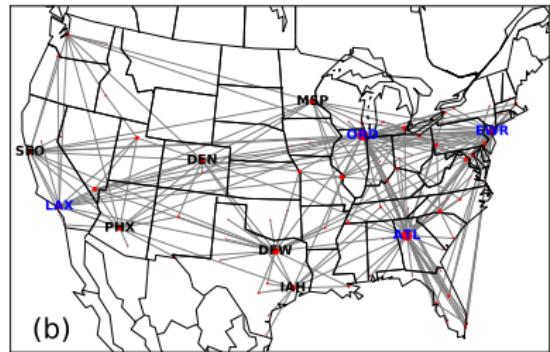
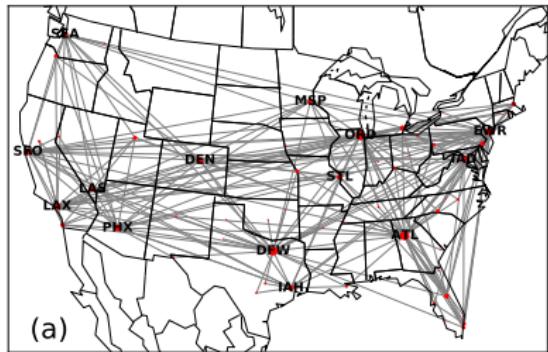
Stay tuned on the arXiv ...



# Global vs Local filtering

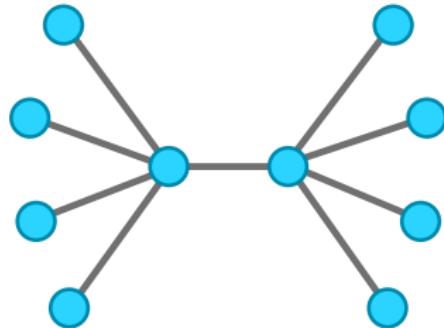


# US Airports



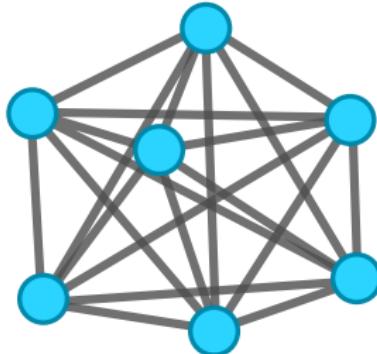


US Airports



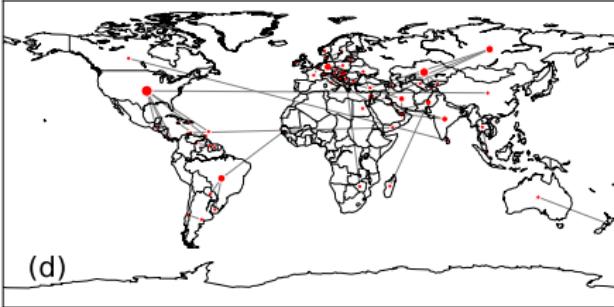
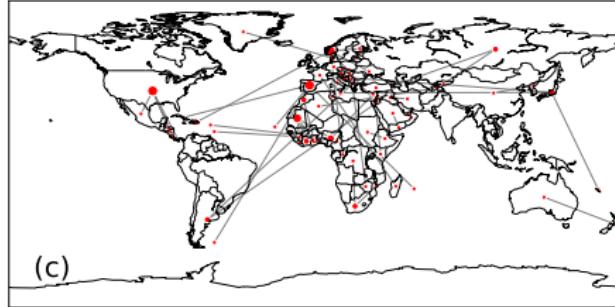
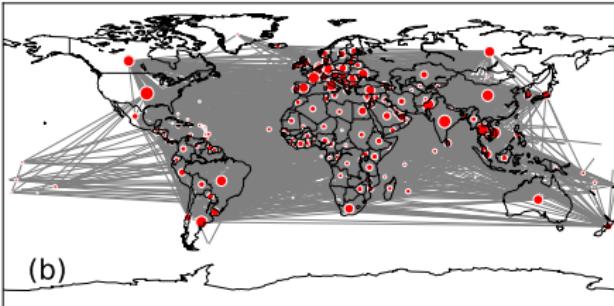
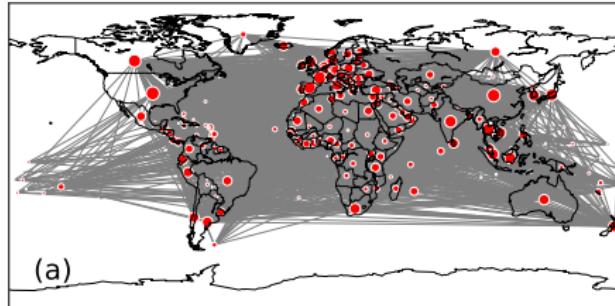
**Hub and Spoke**

**Point to Point**



# Trade: single commodities

## FISH – CEREALS in 2011



# Trade: single commodities

FUEL – IRON in 2011

